



Examination No. 32-821075

Roll No: \_\_\_\_\_

**IIT-JEECH**
**(TERM II) THEORY EXAMINATION 2021-22**  
**ELEMENTARY MATHEMATICS - II**

Time: 3 Hours

Total Marks: 100

Notes:-

- Attempt all sections and answer any missing data.
- Appropriate marks are allotted to each question, answer accordingly.

SECTION - A	Attempt all of following questions in brief	Marks (10+2+2x9)	CO
Q.1(a)	Find $\int \cos^3 x e^{3\sin x} dx$	1	
Q.1(b)	Evaluate $\int_{-\pi}^{\pi} x^{1/2} \cos^2 x dx$	1	
Q.1(c)	Form the differential equation of the family of circles touching the x-axis at origin.	2	
Q.1(d)	In a bank, principal increases continuously at 5% per year. In how many years Rs 1000 double itself?	2	
Q.1(e)	Write all the unit vectors in XY-plane.	3	
Q.1(f)	Find the value of $\alpha$ for which $\alpha(\hat{i} + \hat{j} + \hat{k})$ is a unit vector.	3	
Q.1(g)	Find the coordinates of the point where the line through the points A (3, -4, 1) and B (5, 1, 6) crosses the xy-plane.	4	
Q.1(h)	Find the direction cosines of the sides of the triangle whose vertices are (3, 5, -4), (-1, 1, 3) and (-5, -5, 2).	4	
Q.1(i)	Three cards are drawn successively, without replacement from a pack of 52 well shuffled cards. What is the probability that these cards are jacks and the third card drawn is an ace?	5	
Q.1(j)	Two cards are drawn successively with replacement from a well-shuffled deck of 52 cards. Find the probability distribution of the number of aces.	5	
SECTION - B	Attempt any three of the following questions	Marks (2+3+3x6)	CO
Q.2(a)	Find the area lying above $x = \cos x$ and included between the circle $x^2 + y^2 = 16$ and inside of the parabola $y^2 = 4x$ .	3	
Q.2(b)	Find the equation of a curve passing through the point (0, 1). If the slope of the tangent to the curve at any point $(x, y)$ is equal to the sum of its x-coordinates (abscissa) and the product of its x-coordinates and y-coordinates (ordinates) of the point.	2	
Q.2(c)	Show that the points A (1, -2, -8), B (3, 0, -2) and C (1, 3, 7) are collinear, and find the ratio in which B divides AC.	3	
Q.2(d)	Find the distance of the point (-1, 3, -10) from the point of intersection of the line $\ell = (2\hat{i} - \hat{j} + 2\hat{k}) + \lambda(3\hat{i} + 4\hat{j} + 2\hat{k})$ and the plane $\pi: (\hat{i} - \hat{j} + \hat{k}) = 5$ .	4	
Q.2(e)	Bag I contains 3 red and 4 black balls while another Bag II contains 5 red and 6 black balls. One ball is drawn at random from one of the bags and it is found to be red. Find the probability that it was drawn from Bag II.	5	